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# INSTITUTE OF AERONAUTICAL ENGINEERING

(Autonomous)

Four Year B.Tech III Semester End Examinations (Regular) - November, 2018

**Regulation: IARE – R16**

## DISCRETE MATHEMATICAL STRUCTURES

**Time: 3 Hours**

(Common to CSE | IT )

**Max Marks: 70**

**Answer ONE Question from each Unit**

**All Questions Carry Equal Marks**

**All parts of the question must be answered in one place only**

### UNIT – I

1. (a) Show that  $(p \rightarrow (q \rightarrow r)) \rightarrow ((p \rightarrow q) \rightarrow (p \rightarrow r))$  is a Tautology using truth table. [7M]  
 (b) Show that the statement “Every positive integer is the sum of squares of three integers” is false. [7M]
2. (a) Construct the truth table for the formula  $(PVQ) \vee \neg P$ . [7M]  
 (b) Explain about the tautological implications and logical equivalence using theorem. [7M]

### UNIT – II

3. (a) Show that a relation R defined on the set of real numbers as  $(a, b) R (c, d)$  if  $a^2 + b^2 = c^2 + d^2$ . Show that R is an equivalence relation. [7M]  
 (b) Let  $X = \{1, 2, 3, 4\}$  and  $R = \{(x, y) | x > y\}$ . Draw the diagram of the graph R and also give its matrix. [7M]
4. (a) Illustrate the following function definition with graph. Let X and Y be any two sets. A relation f from X to Y is called a function if for every  $x \in X$  there is a unique  $y \in Y$  such that  $(x, y) \in f$ . [7M]  
 (b) Let  $X = \{1, 2, 3\}$ ,  $Y = \{p, q\}$ , and  $Z = \{a, b\}$ . Also let  $f: X \rightarrow Y$  be  $f = \{(1, p), (2, p), (3, q)\}$  and  $g: Y \rightarrow Z$  be given by  $g = \{(p, b), (q, b)\}$ . Find gof. [7M]

### UNIT – III

5. (a) Show that the intersection of any two congruence relations on a set is also a congruence relation. [7M]  
 (b) Let  $(Z_4, +_4)$  and  $(B, +)$  be the algebraic system. Show that  $(B, +)$  is a homomorphic image of  $(Z_4, +_4)$ . [7M]

6. (a) Prove using the theorem by showing that the composition of semi group homomorphism is also a semi group homomorphism. [7M]  
 (b) Let  $(\mathbb{N}, +)$  be the algebraic system of natural numbers. Define an equivalence relation  $E$  on  $\mathbb{N}$  such that  $x_1 E x_2$  iff either  $x_1 - x_2$  or  $x_2 - x_1$  is divisible by 4. Show that  $E$  is a congruence relation and that the homomorphism  $g$  defined is the natural homomorphism associated with  $E$ . [7M]

**UNIT – IV**

7. (a) What is the solution of the recurrence relation  $a_n = 6a_{n-1} - 9a_{n-2}$  for  $n \geq 2$  given that  $a_0 = 1, a_1 = 6$ . [7M]  
 (b) Find the recurrence relation for the Fibonacci sequence. [7M]
8. (a) A computer system considers a string of decimal digits a valid codeword if it contains an even number of 0 digits. For instance, 1230407869 is valid, whereas 120987045608 is not valid. Let  $a_n$  be the number of valid  $n$ -digit codeword's. find the recurrence relation for  $a_n$ . [7M]  
 (b) Find r recurrence relation for  $C_n$ , the number of ways to parenthesize the product of  $n+1$  numbers,  $x_0, x_1 x_2 \dots x_n$ , to specify the order of multiplication. For example,  $C_3=5$  because there are five ways to parenthesize  $x_0, x_1 x_2 x_3$  to determine the order of multiplication:  $((x_0.x_1)x_2).x_3 (x_0.(x_1)x_2).x_3 (x_0. x_1) (x_2).(x_3) x_0.((x_1)x_2).x_3 x_0. (x_1 (x_2 .x_3))$ . [7M]

**UNIT – V**

9. (a) Prove that if  $G$  is connected graph with  $n$  vertices and  $(n-1)$  edges then  $G$  is a tree. [7M]  
 (b) Show that the graphs  $G$  and  $H$  displayed in following Figure 1 are isomorphic. [7M]

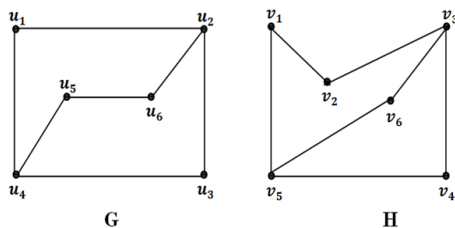


Figure 1

10. (a) Prove that the chromatic number of a tree is always 2 & chromatic polynomial is  $\lambda(\lambda - 1)^{n-1}$ . [7M]  
 (b) Show that neither graph displayed in following Figure 2 has a Hamilton circuit. [7M]

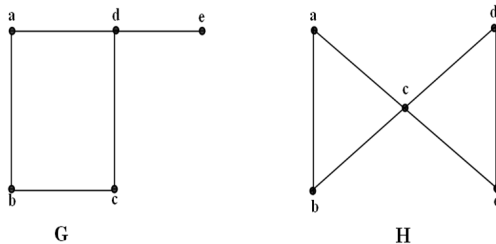


Figure 2

